The crystal structures of pressure-induced LiSrAlF₆-II and LiCaAlF₆-II

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Abstract

The crystal structures of LiCaAlF₆-II and LiSrAlF₆-II (both $P2_1/c$, Z=4) occurring at high pressures and room temperature were studied with synchrotron angle-dispersive x-ray powder diffraction in diamond anvil cells. The structure of LiSrAlF₆-II stable between 1.6 and 3.0 GPa was solved with a global optimisation algorithm and group theory considerations, and refined with the Rietveld method in the rigid-body approximation. It is a distorted variant of the ambient pressure polymorph (LiSrAlF₆-I, $P\bar{3}1c$, Z=2), in which each cation occupies a deformed octahedral site. LiCaAlF₆ transforms to this monoclinic polymorph II above about 7 GPa. The differences in the high-pressure behaviours of LiCaAlF₆ and LiSrAlF₆ are discussed by considering the ionic radii.

1. Introduction

The *colquiriite* family of fluoride compounds LiMM'F₆ (M = Ca or Sr; M' = Al, Ga, or Cr) is considered to be the most promising class of materials for optical applications such as laser hosts and scintillating materials [1–9]. The crystal structure of LiSrAlF₆-I ($P\bar{3}1c$, Z=2) is an ordered derivative of the Li₂ZrF₆ type ($P\bar{3}1m$, Z=1) [10], with each cation occupying a deformed octahedral site within the hexagonal close packed arrangement of fluorine atoms. The polyhedral distortions in LiMM'F₆ have been correlated with the sizes of the M and M' cations [8, 10, 11]. For the M site occupied by luminescent dopants, the distortion, larger for the Sr compounds, is associated with the relative rotations of the two opposite

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trigonal F faces. As a consequence, the strontium-containing materials provide larger optical absorption coefficients determined by the strengths of static and dynamic distortions of the crystal field [11].

Information on the high-pressure behaviour of the *colquiriite* compounds LiMM'F₆ (M = Ca or Sr; M' = Al, Ga, or Cr) is not available in the literature. At high pressures and high temperatures [12, 13], Li₂ZrF₆ transforms into a polymorph with the Li₂TbF₆ structure ($P2_1/c$, Z=4) [14], in which the zirconium atoms have a bicapped trigonal prismatic coordination, forming edge-sharing chains along the a axis. The Li¹⁺ cations are in two types of coordination: octahedra and square pyramids. This structure could be considered a distorted variant of the γ -Na₂UF₆ ordered *fluorite* (*Immm*, Z=2), in which all the cations are surrounded by fluorines in a cube coordination [14]. In the course of our work on the high-pressure high-temperature behaviour of the *colquiriite* compounds LiMM'F₆ (M = Ca or Sr; M' = Al or Ga), we found that LiSrAlF₆ and LiCaAlF₆ undergo a series of reversible pressure-induced structural transformations at room temperature. Here, we investigate the crystal structures of new polymorphs of LiSrAlF₆ occurring below 3.0 GPa and of LiCaAlF₆ formed above about 7 GPa. Additional pressure-induced polymorphs of LiSrAlF₆ above 3 GPa will be the subject of a separate study.

2. Experimental details

Single crystals of LiSrAlF₆ and LiCaAlF₆, grown by the Czochralski method, were ground into fine powders in ethanol and loaded into diamond anvil cells with argon or a silicon oil as the pressure transmitting medium. Angle-dispersive powder x-ray diffraction patterns were measured at room temperature on the Swiss–Norwegian Beamlines at the European Synchrotron Radiation Facility (BM1A, ESRF, Grenoble, France). Monochromatic radiation at 0.719 98 Å was used for data collection on image plate (MAR345). The images were integrated using the program FIT2D [15] to yield intensity versus 2θ diagrams. The ruby luminescence method [16] was used for pressure measurements. At ambient conditions, the measured patterns of LiSrAlF₆ and LiCaAlF₆ matched perfectly those calculated with the program PowderCell [17] using the structural data from Keszler and Schaffers [10]. The refined lattice parameters for LiSrAlF₆ and LiCaAlF₆ were a = 5.1022(1) Å, c = 10.2563(1) Å, V = 229.51(3) Å³, and a = 4.9998(2) Å, c = 9.6418(1) Å, v = 208.73(3) Å³, respectively.

3. Results and discussion

Diffraction patterns of LiSrAlF₆ at selected pressures to 3.0 GPa are shown in figure 1. The diagrams measured between 1.6 and 3.0 GPa are due to a novel high-pressure polymorph of this compound, hereupon called LiSrAlF₆-II. The pattern collected at 1.6 GPa was used for structure determination. The first 20 reflections were indexed using the program DICVOL91 [18] with a monoclinic unit cell: a=10.0560(7) Å, b=8.6197(6) Å, c=5.1367(4) Å, $\beta=91.657(7)^\circ$, V=445.1(2) Å³, M(20)=32.1, F(20)=104.1(0.0035,55). The systematic absences indicated that the space group is $P2_1/a$ (space group no 14) [19]. Unit cells with practically the same volumes, $a\sin\beta$ factors, as well as b and c axial parameters were found by all the routines in the CRYSFIRE suite of indexing programs [20]. The other three diagrams collected at 1.9, 2.4, and 3.0 GPa (figure 1) were also indexed on this $P2_1/a$ unit cell with related, i.e., pressure dependent (figure 2), lattice parameters using the programs DICVOL91 [18], ITO, and TREOR [20].

The crystal structure of LiSrAlF₆-II was partially solved from the pattern collected at 1.6 GPa in the standard $P2_1/c$ (Z=4) setting of space group no 14 with the global optimisation

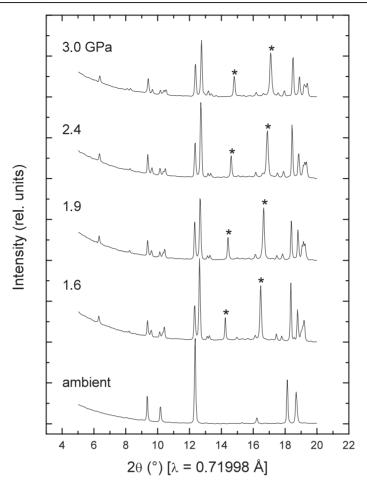


Figure 1. Selected powder patterns of LiSrAlF₆ upon compression with argon as a pressure medium. Reflections due to argon are marked with stars.

algorithm FOX [21]. The lattice parameters in the $P2_1/c$ setting were refined with the Le Bail method [22] as a=5.1346(6) Å, b=8.6283(11) Å, c=10.0598(12) Å, and $\beta=88.362(8)^\circ$. Since the ratio of the number of observed Bragg peaks to the number of structural parameters was expected to be low (52 reflections, all atoms in the general positions 4e), the number of optimized parameters was drastically reduced by introducing an octahedron around the Al atoms with Al–F bond distances equal to 1.78–1.8 Å, i.e., equal to the distances in the ambient pressure structure ($P\bar{3}1c$, Z=2) [10]. The solution was reached in about 50 000 trial configurations. However, the Li atoms could not be properly located using this method and some of the Li–F distances were anomalously short. The entire procedure was repeated without Li atoms and the resulting SrAlF $_6^{-1}$ sublattice was essentially identical. Also, the goodness-of-fit, $R_{\rm wp}$, and $R_{\rm p}$ factors for the calculated and observed patterns were not different. The global optimisation of the LiSrAlF $_6$ -II structure against the diagram collected at 3.0 GPa with such a procedure yielded the same result. During all these procedures bonding and angular distortions of the AF $_6$ octahedra were accounted for by relaxing the delta and sigma parameters in the program FOX [21].

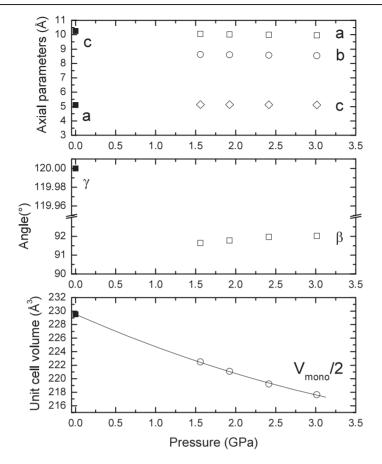


Figure 2. The pressure dependence of unit cell parameters and volumes in LiSrAlF₆ to 3.0 GPa. Full and open symbols stand for the $P\bar{3}1c$ (Z=2) and $P2_1/a$ (Z=4) polymorphs, respectively. For clarity, the unit cell volumes of the monoclinic phase are divided by a factor of two. The line represents the equation-of-state fit to the unit cell volumes.

The detailed analysis of the globally optimised $SrAlF_6^{-1}$ substructure in $P2_1/c$ (Z=4) at 1.6 GPa indicated that it is similar to the one in the $P\bar{3}1c$ (Z=2) structure at ambient conditions [10], with both Sr^{2+} and Al^{3+} cations in distorted octahedral coordination by fluorines. Exploring different possible routes for crystal structure transformations implemented in the program PowderCell [17], it appears that the transformation from the $P\bar{3}1c$ (Z=2) to $P2_1/c$ (Z=4) structures can be derived through the C2/c (Z=4) intermediate. The space group C2/c is the *translationengleiche* subgroup of $P\bar{3}1c$ with the axis transformation (-a-b, a-b, c). Furthermore, the space group $P2_1/c$ is the *klassengleiche* subgroup (type IIa) of C2/c with the axis transformation (a, b, c). The relationship between the hexagonal and monoclinic unit cell parameters is $a_m \approx a_h$, $a_m \approx \sqrt{3}a_h$, $a_m \approx c_h$, with $a_m \approx 2$ 0. It turned out that the positional parameters for Sr, Al, and F atoms in $a_m \approx 2$ 1. Transformed from the $a_m \approx 2$ 2 structure approximated the ones from the structure solution with the global optimization method [21]. Therefore, the Li fractional coordinates in LiSrAlF6-II ($a_m \approx 2$ 2) were derived from the $a_m \approx 2$ 3 structure by the same transformation.

The complete LiSrAlF₆-II structural model, i.e., the globally optimised $SrAlF_6^{-1}$ substructure and the Li¹⁺ cations from group theory considerations, was subsequently used for

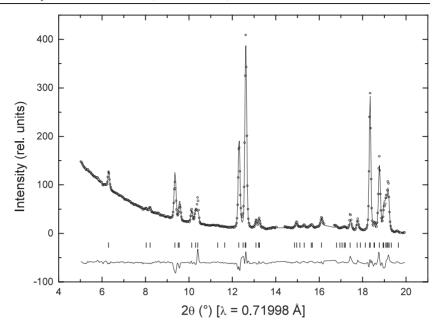


Figure 3. Observed, calculated, and difference x-ray powder patterns for LiSrAlF₆-II $(P2_1/c, Z=4)$ at 1.6 GPa. Vertical markers indicate Bragg reflections. The 2θ regions $14.05^{\circ}-14.4^{\circ}$ and $16.25^{\circ}-16.7^{\circ}$, in which two reflections due to argon are observed, were excluded from the Rietveld refinement.

the structure refinement against the observed pattern at 1.6 GPa with the Rietveld method, using the program GSAS [22] (figure 3). The best fit was obtained at $R_{\rm wp}=12.15\%$, $R_{\rm p}=9.0\%$, $R_{\rm prof}=5.17\%$ (the residuals $R_{\rm wp}$ and $R_{\rm p}$ have been calculated with the background eliminated; see the GSAS manual). After a set of positional parameters for all the atoms had been inserted into the experimental file, the GEOMETRY subroutine was used to determine the orthonormal coordinates and rotation angles $R_1(X)$, $R_2(Y)$, and $R_3(Z)$ for the rigid octahedron centred at the Al³⁺ cation. Introducing the AlF₆ polyhedron reduced the number of structural variables. The refined parameters for the rigid body were: $R_1(X)$, $R_2(Y)$, and $R_3(Z)$ rotation angles, T(X), T(Y), and T(Z) translations, and an isotropic translational tensor ($T_{11}=T_{22}=T_{33}$) in the TLS formalism. The additional variables were: Li and Sr atomic positions, lattice parameters, scale factor, and Stephens profile function [23]. The conventional fractional coordinates for all the atoms and selected interatomic distances are given in table 1.

The structure of LiSrAlF₆-II in different crystallographic projections is shown in figure 4. It consists of deformed LiAlF₆ slabs, in which the Li and Al atoms occupy two thirds of octahedral sites in hexagonal close packing of fluorine atoms in the (a, b) plane. The Sr atoms are sandwiched between the slabs on the octahedral sites. The LiF₆ and AlF₆ polyhedra share edges with each other and vertices with the SrF₆ polyhedra. This structure is a distorted variant of parent LiSrAlF₆-I ($P\bar{3}1c$, Z=2) with the same stacking sequence \cdots F(Li, Al)FSrF \cdots along the c axis [10]. The pressure-induced structure of LiSrAlF₆-II ($P2_1/c$, Z=4) arises from distortions of hexagonal close packing of the fluorine atoms (figures 4 and 5). The comparison of the octahedra around the Sr atoms in the low- and high-pressure phases is shown in figure 5. In the *colquiriite* structure ($P\bar{3}1c$, Z=2), the twisting of the trigonal F planes perpendicular to the C_3 symmetry axis can be described by an angular deviation $\Delta\theta$ from the ideal value of 60°, that is 7.2° in LiSrAlF₆-I [10]. The octahedral distortion in LiSrAlF₆-II ($P2_1/c$, Z=4) can no longer be described by only one $\Delta\theta$ parameter since pairs

Table 1. Structural parameters of LiSrAlF₆-II ($P2_1/c$, Z=4) at 1.6 GPa—a=5.1346(6) Å, b=8.6283(11) Å, c=10.0598(12) Å, $\beta=88.362(8)^\circ$. Estimated standard deviations are given in parentheses.

Atom	X	у	z
Li	0.25(6)	0.581(24)	0.249(27)
Sr	0.2613(24)	0.2195(9)	0.5024(18)
Al	0.271(5)	0.5804(28)	0.7594(19)
F1	0.169(6)	0.7392(34)	0.8654(31)
F2	0.549(6)	0.5476(40)	0.8621(25)
F3	0.444(6)	0.7141(35)	0.6565(28)
F4	-0.010(6)	0.6045(41)	0.6563(25)
F5	0.079(6)	0.4483(34)	0.8614(27)
F6	0.382(7)	0.4259(35)	0.6559(29)
Selected distances (Å)			
Li–F1	1.97(22)	Li–F2	1.87(25)
Li-F3	2.22(22)	Li–F4	2.22(24)
Li-F5	2.06(29)	Li-F6	2.15(29)
$\langle LiF\rangle$	2.08		
Sr-F1	2.555(28)	Sr-F2	2.254(33)
Sr-F3	2.242(26)	Sr-F4	2.578(31)
Sr-F5	2.250(31)	Sr-F6	2.448(29)
$\langle Sr-F \rangle$	2.43		
Al-F1	1.803 62(16)	Al-F2	1.81179(19)
Al-F3	1.774 37(15)	Al-F4	1.809 81(19)
Al-F5	1.807 44(15)	Al-F6	1.776 00(16)
$\langle Al-F \rangle$	1.80		
F1-F2	2.557 47(22)	F1-F3	2.507 61(28)
F1-F4	2.594 52(24)	F1-F5	2.554 05(32)
F2-F3	2.587 24(23)	F2-F5	2.566 03(27)
F2-F6	2.500 19(24)	F3-F4	2.517 42(26)
F3-F6	2.507 95(32)	F4-F5	2.516 24(23)
F4-F6	2.532 55(22)	F5-F6	2.559 86(28)
$\langle F - F \rangle$	2.54		

of opposite F planes in the SrF_6 octahedra are not parallel to each other any more. This new structure of LiSrAlF₆ ($P2_1/c$, Z=4) is different from the monoclinic structures ($P2_1/c$, Z=4) of LiBaMF₆ (M = Al, Ga, Cr, V, Fe, Ti) containing icosahedra of BaF₁₂ within a framework of isolated LiF₄ tetrahedra and MF₆ octahedra mutually linked by corners [24]. It also does not bear any resemblance to the high-pressure high-temperature structure ($P2_1/c$, Z=4) of parent Li₂ZrF₆ [13], with the zirconium atoms in edge-sharing bicapped trigonal prisms along the a axis and the lithium atoms in two types of coordination: octahedra and square pyramids.

The pressure dependence of the lattice parameters in the hexagonal and monoclinic polymorphs of LiSrAlF₆ is plotted up to about 3 GPa in figure 2. The compression data for both $P\bar{3}1c$ (Z=2) and $P2_1/a$ (Z=4) polymorphs to 3 GPa could be fitted together by the Birch equation of state $P(V)=1.5B_0$ ($x^{-7}-x^{-5}$) (1-y), where $x=(V/V_0)^{1/3}$ and $y=0.75(4-B')(x^{-2}-1)$ [25]. Since the number of data points for such a small pressure range was limited, the first derivative of the bulk modulus B' and the V_0 unit cell volume of LiSrAlF₆ at ambient pressure were fixed to 4.0 and 229.51 Å³, respectively, and not refined.

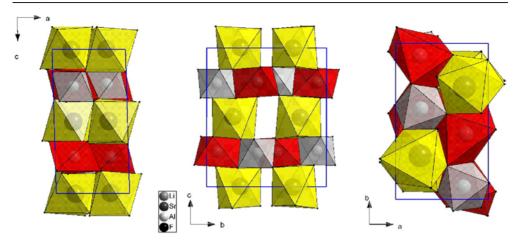


Figure 4. The crystal structure of LiSrAlF₆-II ($P2_1/c$, Z=4). (This figure is in colour only in the electronic version)

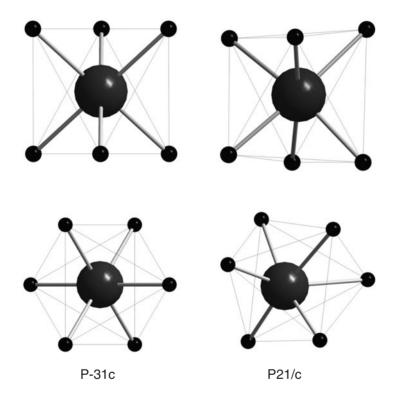


Figure 5. Coordination polyhedra around the Sr atoms in the $P\bar{3}1c$ (left) and $P2_1/c$ (right) polymorphs of LiSrAlF₆.

The resulting zero-pressure bulk modulus B_0 is 49(1) GPa, assuming that the $P2_1/a$ (Z=4) unit cell volumes are divided by a factor of two.

Diffraction patterns of LiCaAlF₆ at selected pressures with a silicon oil or argon as the pressure transmitting medium are shown in figures 6 and 7, respectively. Regardless

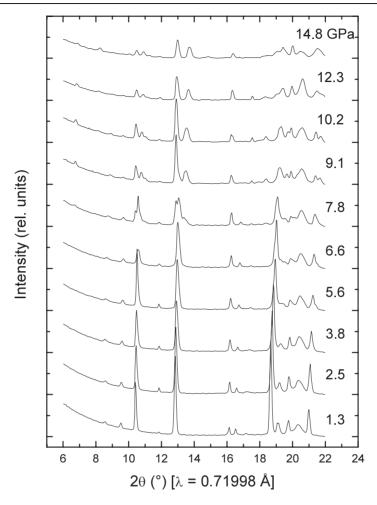


Figure 6. Selected powder patterns of $LiCaAlF_6$ upon compression with a silicon oil as a pressure medium.

of the medium, a fully reversible pressure-induced phase transition in this material takes place above 7 GPa. The low- and high-pressure phases coexist in the range from 7 to about 9 GPa. The first 20 reflections of the pattern collected at 9.1 GPa with argon were indexed using the program DICVOL91 [18] with a monoclinic unit cell: a = 5.0136(5) Å, b = 8.1588(7) Å, c = 9.1821(9) Å, $\beta = 93.08(1)^{\circ}$, V = 375.0(2) Å³, M(20) = 21.6, F(20) = 50.2(0.0056, 68). The systematic absences indicated that the space group is $P_{1/c}$ (space group no 14) [19]. The same unit cell was found by the program TREOR in the CRYSFIRE suite of indexing programs [20]. The unit cell parameters and space group $P_{1/c}$ (Z = 4) suggest that the new structure of LiCaAlF₆ is of the LiSrAlF₆-II type. Indeed, the calculated pattern with the LiSrAlF₆-II structural model matches very well the measured one at 9.1 GPa with argon. In addition, a global optimization method [21] on this diagram yielded the CaAlF₆⁻¹ sublattice like the SrAlF₆⁻¹ one in LiSrAlF₆-II. However, broadening of the observed x-ray reflections precluded any reliable Rietveld refinement [22]. This new polymorph of LiCaAlF₆ is stable at least up to about 16 GPa (figure 7).

The pressure dependence of the lattice parameters in the hexagonal and monoclinic polymorphs of LiCaAlF₆ is plotted in figure 8, assuming that the $P2_1/c$ (Z=4) unit cell

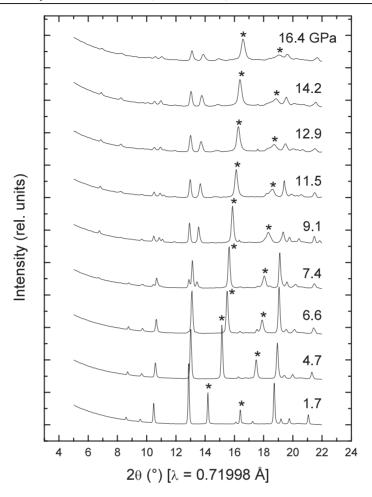


Figure 7. Selected powder patterns of LiCaAlF₆ upon compression with argon as a pressure medium. Reflections due to argon are marked with stars.

volumes are divided by a factor of two. The compression data for the $P\bar{3}1c$ (Z=2) polymorph were fitted by the Birch equation of state [25] with the first derivative of the bulk modulus B' and the V_0 unit cell volume of LiCaAlF₆ at ambient pressure fixed to 4.0 and 208.73 Å³, respectively, and not refined. The resulting zero-pressure bulk modulus B_0 is 93(4) GPa. All the compression data for both the hexagonal and monoclinic polymorphs cannot be fitted by a common equation of state since there is a discontinuity in the evolution of the unit cell volumes at the phase transition $P\bar{3}1c$ (Z=2) $\rightarrow P2_1/c$ (Z=4).

4. Concluding remarks

The combination of a global optimisation [21] and group theory [17] with the Rietveld method [22] allowed for the solution and refinement of the crystal structure of high-pressure LiSrAlF₆-II ($P2_1/c$, Z=4) from x-ray powder diffraction data. Important for the successful solution and refinement was the introduction of the rigid-body geometrical constraints to AlF₆ octahedral units, resulting in a reduced number of structural variables. The structure of the

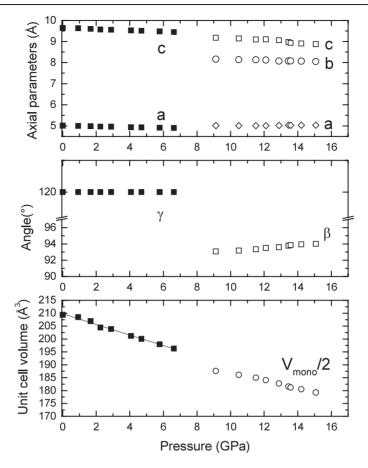


Figure 8. The pressure dependence of unit cell parameters and volumes in LiCaAlF₆. Full and open symbols stand for the $P\bar{3}1c$ (Z=2) and $P2_1/a$ (Z=4) polymorphs, respectively. For clarity, the unit cell volumes of the monoclinic phase are divided by a factor of two. The line represents the equation-of-state fit to the unit cell volumes. The data for the two phases coexisting in the pressure range 7–9 GPa are not plotted.

LiSrAlF₆-II polymorph ($P2_1/c$, Z=4) below 3.0 GPa is a distorted variant of LiSrAlF₆-I ($P\bar{3}1c$, Z=2) and consists of deformed LiAlF₆ slabs, in which the Li and Al atoms occupy two thirds of the octahedral sites in hexagonal close packing of fluorine atoms. This LiSrAlF₆-II-type structure type is also taken by LiCaAlF₆ at pressures exceeding 7 GPa and is stable at least up to about 16 GPa.

The stability and distortions of the *colquiriite* structure at atmospheric conditions have been previously discussed on a basis of ionic radii [8, 10, 11]. The Ca²⁺ and Sr²⁺ cations are octahedrally coordinated to fluorines. The octahedral distortions are larger for the Sr compounds and are associated with the relative rotations of the two opposite trigonal F faces. The compounds LiBaMF₆ (M = Al, Ga, Cr, V, Fe, Ti) do not possess the *colquiriite* structure ($P2_1/c$, Z=4) as icosahedra of BaF₁₂ are within a framework of isolated LiF₄ tetrahedra and MF₆ octahedra linked by corners [24]. Another structural type is encountered in LiSmAlF₆ ($P6_322$, Z=2) that is derived from the LiSrAlF₆-I type ($P\overline{3}1c$, Z=2), however with Sm²⁺ in a trigonal prismatic coordination to fluorine atoms [26]. Accordingly, the observation that up to 3.0 GPa LiSrAlF₆ has the $P2_1/c$ (Z=4) structure with all the cations in the octahedral

coordination while LiCaAlF₆ transforms to the same type above 7 GPa could be explained with the 'ionic radii' argument. Similar distortions in the hexagonal close packing of fluorines and coordination units of the cations like the ones in LiSrAlF₆-II ($P2_1/c$, Z=4) may be expected at low temperatures and atmospheric pressure to explain the anomalies in electron spin-resonance spectra of the solid solution LiSr_xCa_{1-x}AlF₆ [11].

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